

2022 APMCM summary sheet

Global warming is a very serious problem facing human society at present. The research and analysis of global temperature and related factors have become an important topic.

In question 1, we first break down the data in the northern and southern hemispheres and divide the data with March 2022 as the boundary. Subsequently, normality analysis was carried out on the two groups of data respectively. On the premise of meeting normality, difference analysis was carried out and the **rank-sum test** was adopted to calculate the significance of the data. Finally, we decided that we could not agree.

When predicting the future temperature, we set up the **grey prediction model** and the **ARIMA prediction model** to predict the future temperature data respectively. Grey prediction models suggest that global temperatures will reach 20°C in 2215. The ARIMA prediction model predicts it will reach 20° C in 2187. Finally, the accuracy of the two models is tested respectively to ensure the accuracy of the model.

In question 2, in order to explore the relationship between global temperature and time and location, we divided the temperature zone by latitude and time by year, and analyzed the correlation between temperature and location, temperature and time respectively. In order to further study their relationship, we built a **linear regression model**, taking location and time as independent variables respectively, and obtained their linear regression equations of global temperature.

In view of the analysis of the impact of natural disasters on temperature, we selected the corresponding events for specific analysis. By building a grey prediction model to predict the theoretical value of global temperature during and after the occurrence of the event, and comparing it with the real value, it can be concluded that forest fires and volcanic eruptions will increase global temperature to a certain extent, while the COVID-19 pandemic has little impact on the temperature. Continuing the above analysis, we believe that the main factor affecting global temperature is carbon emission, and the **correlation analysis** of the two is strong correlation, which confirms the above view.

Finally, the comprehensive determination model has strong generality.

Keywords: grey prediction model ARIMA prediction model linear regression model

Contents

I. The Restatement of the Problem

1 . 1 Background of the Problem

The average global temperature between *1981* and *1990* was *0.48*℃ higher than *100* years ago. The main cause of global warming is that human beings have been using fossil fuels (such as coal and petroleum) in large quantities in the past century, which has emitted a large amount of $CO₂$ and other greenhouse gases. These greenhouse gases cause global climate warming. During the *20*th century, the world's average temperature rose by about *0.6* degrees Celsius. Spring thaws in the northern Hemisphere are starting nine days earlier than they did *150* years ago, while autumn frosts are starting about *10* days later.

There are many factors contributing to global climate warming, which can be divided into man-made factors and natural factors. Human factors include population increase, air pollution, forest resource reduction, and natural factors include volcanic activity.

1 . 2 Presentation of the Problem

In order to further explore the problem of global warming, the question asks to build a mathematical model based on relevant data to study the following problems:

- Analyze temperature data to determine whether the increase in global temperatures in March *2022* has resulted in a greater increase than in the previous *10* years; Build two prediction models to predict future global temperature levels; By predicting the temperature data in *2050* and *2100* through the prediction model, we can find out whether it will reach *20*°C, if not, when it will reach *20*°C. Check the accuracy of the prediction model to ensure its accuracy.
- Analyze the relationship between global temperature, time and location by combining corresponding data; Analyzing the impact of natural disasters (volcanic eruptions, forest fires, COVID-*19*) on temperature; Explore the main factors affecting global temperature; To provide measures to mitigate global warming.

II. Analysis of Problems

2 . 1 Analysis of Problem One

Problem One requires an analysis of whether the rise in global temperatures in March *2022* has led to a larger increase than in the previous decade. In this regard, we first preprocessed the data, divided the northern and southern hemispheres according to latitude, and analyzed the normality of the two groups of data respectively to ensure that the data set met the normal distribution curve. Then, we conducted the rank sum test to analyze the differences and reached the corresponding conclusions.

For the construction of prediction model. We have established the grey prediction model and the ARIMA prediction model successively, and completed the forecast of the weather data in *2050* and *2100*, and reached the corresponding conclusions.

Finally, the accuracy of the grey model was tested and the error analysis of the ARIMA model was carried out to ensure the accuracy of the prediction model.

2 . 2 Analysis of Problem Two

In Problem Two, we need to explore the relationship between global temperature and time and location. We further divide the data according to the temperature zone, and use correlation analysis to preliminarily test the relationship between the temperature and the two. In order to further study the specific functional relationship, we establish a linear regression model to obtain the specific relationship between the global temperature and the two.

When analyzing the impact of natural disasters on global temperature, we collected the data of specific volcanic eruptions, forest fires and COVID-*19*. The grey prediction model established in Problem One was used to predict the theoretical temperature at the time of the event, and then compared it with the real data to get the corresponding conclusions.

After the preliminary conclusion that carbon emissions may be the main reason affecting temperature, we collected the global carbon emissions data, conducted correlation analysis between them and the global temperature value, tested the degree of correlation between them, and then reached an accurate conclusion. Finally, we offer solutions to the main causes of global warming.

III. Model Assumptions

- **1:** The global temperature is considered to be the average temperature of the northern and southern hemispheres, ignoring the influence of special factors.
- **2:** In the analysis of location, it is considered that the south temperate zone, the tropical zone and the north temperate zone are the main factors, and the influence of temperature in the two cold zones is ignored.
- **3:** Considers the global temperature data provided to be true and reliable.

IV. Terms, Definitions and Symbols

V. Data Processing

5 . 1 Data Screening

The attached data set contains temperature data for cities and countries from *1743* to *2013*.As the topic of this paper is global warming, various factors affecting global warming need to be taken into account. After the second Industrial Revolution, the emergence of electricity and the wide application of electrical appliances have made great progress in productivity, and it is because of this that the problem of global warming appears. In addition, due to problems such as serious missing and poor continuity of data dating back to a long time ago, based on the above considerations, our team chose the time of the second Industrial Revolution as the turning point, and only selected the temperature data of *1888* and later as the research object, excluding other data.

5 . 2 Missing value processing

There were some missing months in the data set.Considering that the temperature of adjacent months showed a certain trend of rising or falling, we used the average temperature of adjacent two months to complete the missing values.

VI. Model Building, Solving and Analyzing of Problem

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6 . 1 Analysis of Temperature Rise

6 . 1 . 1 *Data Preprocessing*

In the relevant analysis of the temperature rise in this problem, considering that the temperature characteristics of different months in the northern and southern hemispheres are quite different, we divide the northern and southern hemispheres by latitude and classify the data for better discussion and analysis.

Figure 6.1 Temperature Trend Chart of the Northern and Southern Hemispheres

As can be seen from the temperature trend chart of the northern and southern hemispheres above, the global temperature rise in March *2022* shows no significant difference between the two hemispheres compared with the previous decade. Next, we will analyze the difference of the corresponding data to get a more accurate conclusion.

6 . 1 . 2 *Difference Analysis*

In order to more intuitively observe the difference of temperature rise, we separated two sets of data from the northern and southern hemispheres using March *2022* temperature as the boundary, and further analyzed the difference using Mann-Whitney U-tests.

Before conducting Mann-Whitney U-tests, normality analysis of the data set is required to ensure that it basically meets the normal distribution before proceeding to the next step.

Figure 6.2 Normal distribution curve

The figure above shows the results of data normality test. The normal graph basically presents a bell shape (high in the middle and low at both ends), indicating that although the data is not absolutely normal, it can be basically accepted as normal distribution, so the following steps can be carried out.

In the temperature samples of the Southern Hemisphere, let the data quantity of the two samples be n_1 and n_2 respectively, and let R_1 represent the rank sum of sample *1* and R_2 represent the rank sum of sample 2[1].

$$
U_1 = n_1 n_2 + \frac{n_1 (n_1 + 1)}{2} - R_1
$$

\n
$$
U_2 = n_1 n_2 + \frac{n_2 (n_2 + 1)}{2} - R_2
$$
\n(1)

At the time of inspection, let: $U = min (u_1, u_2)$, when the sample is large

$$
\mu_{\rm u} = \text{mn}/2,
$$

$$
\sigma_{\mu} = \sqrt{n_1 n_2 (n_1 + n_2 + 1) / 12}
$$
 (2)

The sampling distribution of U rapidly approaches the normal distribution:

$$
Z = \frac{\left|U - \frac{n_1 n_2}{2}\right|}{\sqrt{\frac{n_1 n_2 (n_1 + n_2 + 1)}{1}}}
$$
(3)

After obtaining the Z value, the significance of mean difference between the two samples can be judged by looking up the table.

Note: ***, ** and * represent the significance level of 1%, 5% and 10% respectively

Table 6.3 MannWhitney U Test Analysis Results

In the above table, the P values of both hemispheres are greater than *0.05*, so there is no significant difference between the temperature values of March *2022* in the southern Hemisphere and the Northern Hemisphere.

6 . 1 . 3 *Conclusion*

According to the above difference analysis, compared with the past decade, the global temperature rise in March *2022* shows no significant difference, so we do not agree with the statement of temperature rise.

6 . 2 Temperature Forecasting Problem

6 . 2 . 1 *Data Preprocessing*

For the temperature Forecasting problem, instead of using monthly data, we integrate the temperature of the northern and southern hemispheres separately and take the average value to obtain the annual average data of the year for subsequent prediction model construction and calculation.

6 . 2 . 2 *Construction and Analysis of Grey Prediction Model*

The $GM(1, 1)$ model is the most widely used in grey prediction, and the prediction of data can often get more accurate results.Before this, it is necessary to conduct grade-ratio test for time series, and only the series that pass the grade-ratio test can be predicted and analyzed by grey model. If it does not pass the stage ratio test, "translation conversion" is performed on the sequence, so that the new sequence meets the stage ratio test. Finally, all the stage ratios must be in the interval $\left(e^{\frac{-2}{n+1}}, e^{\frac{-2}{n+1}}\right)$ to pass the test. Due to the complexity of the data, the results of the initial stage ratio test and the test results after translation and conversion will be shown in the appendix. The grey prediction model will be established below.

With the original data sequence : $X^{(0)}(1), X^{(0)}(2), ..., X^{(0)}(n)$, they satisfy $X^{(0)}(k) \geq$ $0, k = 1, 2, \ldots, n$ The general steps for establishing a $GM(1, 1)$ model with this data series are:

1) Make first-order accumulation to generate data series

$$
X^{(1)}(k) = \sum_{m=1}^{k} X^{(0)}(m), \quad k = 1, 2, \dots, n
$$
 (1)

2) Determine the data matrix $B_{1}Y_{n}$

$$
B = \begin{pmatrix} -\frac{1}{2} \left[X^{(1)}(1) + X^{(1)}(2) \right] & 1 \\ -\frac{1}{2} \left[X^{(1)}(2) + X^{(1)}(3) \right] & 1 \\ \cdots & \cdots & \cdots \\ \frac{1}{2} \left[X^{(1)}(n-1) + X^{(1)}(n) \right] & 1 \end{pmatrix}, \quad Y_n = \begin{pmatrix} X^{(0)}(2) \\ X^{(0)}(3) \\ \cdots \\ X^{(0)}(n) \end{pmatrix}
$$
(2)

3) Find the parameter column

$$
\left[\widehat{a}\widehat{u}\right]^T = \left(B^T B\right)^{-1} B^T Y_n \tag{3}
$$

4) Build the model of generating data series

$$
\widehat{X^{(1)}}(k+1) = \left(X^{(0)}(1) - \frac{u}{a}\right) e^{-\widehat{ak}} + \frac{\widehat{u}}{\widehat{a}} \quad k = 1, 2, \dots
$$

5) Establish the original data series model

$$
\widehat{X^{(0)}}(1) = X^{(0)}(1)
$$

$$
\widehat{X^{(0)}}(k) = \widehat{X}^{(1)}(k) - \widehat{X}^{(1)}(k-1)
$$

$$
= \left(1 - e^{\widehat{a}}\right) \left(X^{(0)}(1) - \frac{u}{a}\right) e^{-\widehat{a(k-1)}}, \quad k = 2, 3, \dots \tag{4}
$$

Here, $X^{(0)}(k)$ $(k = 1, 2, ..., n)$ is the original data sequence $X^{(0)}(k)$ $(k = 1, 2, ..., n)$ fitting values, $\overline{X}^{(0)}$ (k) (k > n) is the predictive value of the original data sequence[2].

Using the grey prediction model to predict the future data, we obtained the future temperature model fitting forecast maps for the northern and southern hemispheres respectively.

Figure 6.4 Grey prediction model fitting prediction graph

6 . 2 . 3 *ARIMA Model Prediction*

The following process is required to predict time series using the ARIMA model.

Firstly, the original time series data is preprocessed, and all of them are zero-valued.

Let the original sequence be the mean of $\{y(t)\}\$, the mean of $\{y(t)\}\$ $\bar{y} = \frac{1}{n}$. Let the sample value of the new sequence $x(t) = y(t) - \overline{y}$.

The number of differential processing is determined by the parameter d in the $ARIMA(p, d, 0)$ model structure: $d = 1$, one differential processing, $d = 2$, two differential processing, and so on. If $d = 0$, that is, no differential processing is carried out, and the model structure is $AR(p)$.

If the model of the new sequence obtained after d difference of the original sequence is $AR(p)$ model, then the original sequence is $ARIMA(p, d, 0)$ model. The parameter estimation and prediction described below are carried out for the $AR(p)$ model after differential processing, and the prediction value of the original sequence can be obtained by inverse transformation after the prediction result is obtained.

Then the parameter estimation work is carried out.

The recursive least squares method with forgetting factor was used for parameter estimation. The role of forgetting factor is to strengthen the effect of current observation data on parameter estimation, while weaken the influence of previous observation data. The forgetting factor mainly considers the time variation of model parameters[3].

The mathematical expression of AR (p) model of sequence {y(t)} is as follows:

$$
A(B) y(t) = e(t)
$$
 (1)

Among them, the $e(t)$ is the white noise of zero mean, B is the backward operator, and $A(B)$ is the same as equation (1). Then equation (2) can be written as:

$$
y(t) = a_1y(t-1) + a_2y(t-2) + \ldots + a_yy(t-p) + c(t)
$$

Written in vector form:

$$
y(t) = \varphi^T(t)\theta + e(t)
$$

Among them

$$
\varphi^{T}(t) = [y(t-1), y(t-2), \cdots, y(t-p)]
$$

$$
\theta = [a_{1}, a_{2}, \dots, a_{p}]^{T}
$$
(2)

Substitute $\varphi^{T}(t)$, θ into the formula of recursive least squares method with forgetting factor; With initial values, the online recursive parameter estimation can be carried out.

Finally, to complete the prediction of the model.

Astrom prediction method based on the linear least variance prediction principle is used to predict. This algorithm can solve the problem of large randomness in the prediction. Description form as follows:

For a stationary reversible $ARMA(p, q)$ process:

$$
A(B) y(t) = C(B) e(t)
$$

Where B is backward shift operator, $A(B)$ and $C(B)$ are the same as equation (1), and the minimum variance predictor is:

$$
\hat{y}(t+k \mid t) = (G(B)/C(B))y(t)
$$

Its recursive form:

$$
C(B)\hat{y}(t+k \mid t) = G(B)y(t)
$$

Where $G(B)$ and $F(B)$ can be obtained by the Diophantine equation as follows:

$$
C(B) = A(B)F(B) + B^{k}G(B)
$$

In the equation

$$
F(B) = f_0 + f_1 B + f_2 B^2 + \dots + f_{nj} B^{nf}
$$

\n
$$
G(B) = g_0 + g_1 B + g_2 B^2 + \dots + g_{kg} B^{ng}
$$
\n(3)

 $nf = k - 1, ng = max (p - 1, q - k)$. This paper is a one-step prediction algorithm. It only needs to substitute $C(B) = 1, q = 0$ and the number of prediction steps $k = 1$ into the above formula. After simple derivation and calculation, the one-step prediction formula can be obtained.

Using the ARIMA model, we get future temperature projections for the northern and southern hemispheres.

Figure 6.5 ARIMA prediction model fitting prediction diagram

6 . 3 Future Prediction and Result Analysis

The grey prediction model and ARIMA prediction model are respectively applied, and the following prediction data can be obtained after *2050* and *2100* are substituted into the model.

Mode1	Grey prediction				ARIMA prediction			
Region				Southern Hemisphere Northern Hemisphere Southern Hemisphere Northern Hemisphere				
Year	2050	2100	2050	2100	2050	2100	2050	2100
Predicted Temperature/ $^{\circ}$ C	18.54	19.64	15.21	17.29	18.71	19.95	15.74	17.3

Table 6.6 Future temperature forecast results

As can be seen from the above table, the annual mean temperature will not reach *20*°C in either *2050* or *2100*, nor in the Southern Hemisphere or the Northern Hemisphere. Therefore, we disagree with this statement.

In order to calculate when the global annual mean temperature will reach *20*°C, we average the northern and southern hemispheres of the two models respectively to better observe the change in global temperature values. Each model predicts the annual mean temperature for the next *500* years. Due to the complexity of the data, the detailed forecast results are presented in the appendix.

Through the prediction of the two models, the grey prediction model shows that the global temperature in *2215* is *20.04*°C, reaching *20*°C for the first time. The ARIMA forecast model says the global temperature will be *20.00*°C in 2187, reaching *20*°C for the first time.

6 . 4 Accuracy Test

6 . 4 . 1 *Accuracy Test of Grey Prediction*

This paper uses the posterior error method to test the accuracy of the grey prediction model $GM(1, 1)$. According to the classification standard of the accuracy grade of the grey prediction model, the following classification table is obtained[4].

Note: *c* is the posterior difference ratio, $c = \frac{s_2}{s_1}$, *P* is the small error probability.

Table 6.7 Standard for Determining Accuracy Level of Model

Then we need to calculate the posterior difference ratio and the small error probability.

First of all, we need to calculate the residual $\varepsilon(k)$.

$$
\varepsilon(k) = X^{(0)}(k) - x^{(0)}(k), k = 2, 3, \cdots, n
$$
 (1)

Then calculate the relative error $\Delta(k)$.

$$
\Delta(k) = \frac{|\varepsilon(k)|}{X(0)(k)}, k = 2, 3, \cdots, n
$$
 (2)

And then calculate the standard deviation of the original sequence S_1 and the standard deviation of the residual sequence S_2

$$
S_1 = \sqrt{\frac{1}{n} \sum_{k=2}^{n} \left[X^{(0)}(k) - X \right]}
$$

$$
S_2 = \sqrt{\frac{1}{n} \sum_{k=2}^{n} \left[\Delta(k) - \Delta \right]}
$$
 (3)

Then variance ratio C

$$
C = \frac{S_2}{S_1}
$$

Small probability error P

$$
P = P\left\{ |\Delta(k) - \Delta| < 0.6745S_2 \right\}, k = 2, 3, \cdots, n \tag{4}
$$

The accuracy of model fitting is determined by C and P .

After the model accuracy test of the sample set, it is obtained that the mean residual $\bar{\epsilon}$ =-19.92, the variance of residual ϵ^2 =4333.97, the posterior difference ratio $c=0.27<0.35$, and the small probability error $p=0.984\geq0.95$. The prediction grade of the model is level 1, the prediction results are reliable and the model is relatively accurate.

6 . 4 . 2 *ARIMA error analysis*

In order to evaluate and compare the results predicted by the model, the following two indicators are used in this paper.

(1) Relative error, represented by RE, can describe the quality of prediction effect at a certain moment. The calculation formula is as follows:

$$
RE(t) = [y(t) - \hat{y}(t)] / y(t)
$$
\n(1)

Where $y(t)$ is the measured value, $\hat{y}(t)$ is the predicted value;

(2) MAPE(mean absolute percentage error), which is an indicator to comprehensively evaluate the prediction performance of the whole prediction process, is calculated as follows:

$$
MAPE = \frac{1}{n} \sum_{t=1}^{n} |RE(t)|
$$
 (2)

Where $RE(t)$ is the relative error at time t and n is the number of samples.

With MAPE as the evaluation index, we randomly selected *14* samples from the original data set for error test and analysis.

Table 6.8 Random sample error analysis

According to the error test results of random samples, the value of MAPE is basically stable below *5*%, indicating that the model prediction simulation results are excellent, has good adaptability, and the model is more accurate.

VII. Model Building, Solving and Analyzing of Problem

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7 . 1 The Correlation of Global Temperature, Time and Location

7 . 1 . 1 *Data Preprocessing*

In order to better study the correlation between global temperature and regional location, the data provided in the annex are divided into specific regions. According to *23.5*°N and *23.5*°S, the temperature data in the annex are further classified into North temperate zone, tropical zone and South temperate zone. Due to the small number of countries in the northern and southern regions, and the temperature conditions are not suitable for the research objects, they are not considered here. Therefore, it is only divided into three temperature zones, and the annual average temperature of each temperature zone is taken for further analysis and processing.

Regarding the analysis of time, we further sorted and classified the data, and explored the relationship between the data and global temperature change with the year as the basis.

7 . 1 . 2 *Correlation Analysis*

The research on correlation analysis between regions and years and global temperature is divided into two studies, and the correlation analysis between regions and temperatures and years and temperatures is conducted twice respectively. Firstly, the Pearson correlation coefficient method is adopted to analyze the degree of pairwise correlation of each temperature zone.

The Pearson correlation coefficient between two variables is defined as the quotient of the covariance and standard deviation between the two variables:

$$
\rho_{X,Y} = \frac{cov(X,Y)}{\sigma_X \sigma_Y} = \frac{E\left[\left(X - \mu_X\right)\left(Y - \mu_Y\right)\right]}{\sigma_X \sigma_Y} \tag{1}
$$

The above equation defines the overall correlation coefficient, which is usually represented by the Greek lowercase letter ρ . To estimate the covariance and standard deviation of the sample, Pearson correlation coefficient can be obtained, commonly represented by the lowercase letter \overline{r} in English:

$$
r = \frac{\sum_{i=1}^{n} (X_i - \bar{X}) (Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^{n} (X_i - \bar{X})^2} \sqrt{\sum_{i=1}^{n} (Y_i - \bar{X})^2}}
$$
(2)

can also be estimated by the mean value of the standard fraction of the sample point (X_i, Y_i) , and the expression equivalent to the above equation can be obtained:

$$
r = \frac{1}{n-1} \sum_{i=1}^{n} \left(\frac{X_i - \bar{X}}{\sigma_X} \right) \left(\frac{Y_i - \bar{Y}}{\sigma_Y} \right)
$$
(3)

Where $\frac{X_i - \bar{X}}{\sigma_X}$, \bar{X} and σ_X are the standard fraction, sample mean and sample standard deviation of the sample of X_i , respectively[5].

The correlation between air temperature and each temperature zone is calculated and expressed in the form of heat map. The process of correlation analysis between time and temperature is repeated.

Figure 7.1 Correlation coefficient heat map

It can be intuitively observed from the correlation coefficient heat map that the global temperature is closely related to the region and time.

7 . 1 . 3 *Linear Regression Model*

According to the above correlation analysis, the correlation is very close. In order to further explore the specific relationship between temperature and region, temperature and time, linear regression is adopted to further solve the problem.

Let the sample point capacity be *n*, the dependent variable at time t be y^t , and the *p* independent variables be x^i \int_{i}^{t} $(j = 1, 2...p)$, then the form of the overall linear regression model is[6]:

$$
y_{i}^{t} = \beta_{0} + \beta_{1}^{t} x_{i1}^{t} + \dots + \beta_{p}^{t} x_{ip}^{t} + \varepsilon_{i}^{t} \quad i = 1, 2, \dots, n
$$
\n
$$
\text{Let's call } \mathbf{y}^{t} = \begin{pmatrix} y_{1}^{t} \\ y_{2}^{t} \\ \vdots \\ y_{n}^{t} \end{pmatrix}_{n \times 1} \beta^{t} = \begin{pmatrix} \beta_{0}^{t} \\ \beta_{1}^{t} \\ \vdots \\ \beta_{p}^{t} \end{pmatrix}_{(p+1) \times 1}
$$
\n
$$
\mathbf{X}^{t} = \begin{pmatrix} 1 & x_{11}^{t} & x_{12}^{t} & \cdots & x_{1p}^{t} \\ 1 & x_{21}^{t} & x_{22}^{t} & \cdots & x_{2p}^{t} \\ \vdots & \vdots & \vdots & \vdots \\ 1 & x_{n1}^{t} & x_{n2}^{t} & \cdots & x_{np}^{t} \end{pmatrix}_{n \times (p+1)}
$$
\n
$$
(1)
$$

Then the cross product V^t of the augmented matrix (X^t, y^t) is

$$
\boldsymbol{V}^{t} = \begin{pmatrix} (\boldsymbol{X}^{t})' \boldsymbol{X}^{t} & (\boldsymbol{X}^{t})' \boldsymbol{y}^{t} \\ (\boldsymbol{y}^{t})' \boldsymbol{X}^{t} & (\boldsymbol{y}^{t})' \boldsymbol{y}^{t} \end{pmatrix} = \begin{pmatrix} \boldsymbol{V}_{11}^{t} & \boldsymbol{V}_{12}^{t} \\ \boldsymbol{V}_{21}^{t} & \boldsymbol{V}_{22}^{t} \end{pmatrix}
$$
(2)

The least squares estimator of regression coefficient β^t is

$$
\widehat{\beta}^t = \left(V_{11}^t\right)^{-1} V_{12}^t \tag{3}
$$

It can also be proved that the values of S_{SSE} and S_{SST} at time t are shown in Equation (11) and Equation (12) respectively.

$$
S_{SSE}^{t} = V_{22}^{t} - V_{21}^{t} (V_{11}^{t})^{-1} V_{12}^{t}
$$
 (4)

$$
S_{SST}^t = V_{22}^t - \frac{1}{n} \left(V_{12,1}^t \right)^2 \tag{5}
$$

Where V_1^t $t'_{12,1}$ is the first component of V_{12}^t . According to equations (11) and (12), the goodness of fit (adjusted complex measurement coefficient) at time t is

$$
\bar{R}_t^2 = 1 - \frac{S_{SSE'}^t(n - p - 1)}{S_{SST'}^t(n - 1)}
$$
\n(6)

Meanwhile, the estimated standard error at time t is

$$
S_e^t = \sqrt{\frac{1}{n - p - 1} S_{SSE}^t}
$$
 (7)

The specific modeling method of linear regression model is as follows:

1) Calculate t ($t = 1, 2,...T$) Cross product V^t of the augmented matrix $(X^t y^t)$) at time;

2) Calculate the eigenvalue of $V^t \lambda^t$ $\lambda_1^t \geq \lambda_2^t$ $\lambda_2^t \geq \ldots \geq \lambda_j^t$ $p_{p+2}^{t} \ge 0$ and the corresponding orthonormal eigenvector u_1^t $u_1^t, u_2^t, \ldots, u_{p+2}^t$ $(t = 1, 2, \ldots, T);$

3) According to the eigenvector matrix of the cross product matrix V^t at the time $1 \sim T$, the orthogonal matrix prediction method is used to predict the eigenvector matrix at the time $T + l \left(u_1^{T+l} \right)$ $T+l$ _u $T+l$ ₂ 2 $T+l$ $p+2$;

4) According to the eigenvalues of the cross product matrix V^t at the time $1 \sim T$, the time series analysis method is applied to predict the eigenvalues at time $T + l$ respectively λ^{T+l} $T+1$ ₁ $T+1$ ₂ $_{2}^{T+l}$... λ_{p+2}^{T+l} ;

5) According to the calculation results of the last two steps, the cross product matrix V^{T+l} at time $T + l$ is calculated as

$$
\mathbf{V}^{T+l} = \begin{pmatrix} \mathbf{u}_1^{T+l} & \mathbf{u}_2^{T+l} & \cdots & \mathbf{u}_{p+2}^{T+l} \end{pmatrix}
$$

$$
\begin{pmatrix} \lambda_1^{T+l} & 0 & 0 & 0 \\ 0 & \lambda_2^{T+l} & \cdots & 0 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & \cdots & \lambda_{p+2}^{T+l} \end{pmatrix} \cdot \begin{pmatrix} \mathbf{u}_1^{T+l} & \mathbf{u}_2^{T+l} & \cdots & \mathbf{u}_{p+2}^{T+l} \end{pmatrix}'
$$

6) According to Equation (3), the estimator $\widehat{\beta}^{T+l}$ of the regression parameter at time $T + l$ can be obtained;

7) According to equations (4) ~ (7), the goodness of fit R_{T+1}^2 and the estimated standard error S_e^{T+1} of the regression model at time T+I can be calculated.

For the relationship between region and temperature, the following results are obtained according to the above process. The above table shows the analysis results of this model, including the standardized coefficient of the model, *t* value, VIF value, R^2 , adjustment R^2 , etc., for the test of the model and the analysis of the formula of the model. F test is to judge whether there is a significant linear relationship, and R^2 is to judge whether the regression line fits the linear model. In linear regression, the main concern is whether the F test is passed, and in some cases, the size of \mathbb{R}^2 is not necessarily related to the model explicity. According to the analysis of the results of F test, the significance

R^2	V_{IF}			normalized coefficient	Non normalized coefficient		
			Beta		Standard error		
		0.321				constant	
	4.051	$0.000***$	0.332		0.333	Xs	
	3.935	$0.000***$	0.408		0.333	Xn	
	4.927	$0.000***$	0.32		0.333	Xt	

Note: ***, ** and * represent the significance level of 1%, 5% and 10% respectively

Table 7.2 Linear regression results analysis table

P value is *0.000****, showing significance at the level, rejecting the null hypothesis that the regression coefficient is 0, so the model basically meets the requirements.

For the collinearity of variables, VIF is all less than *10*, so the model has no multicollinearity problem and the model is well constructed.

The formula of the model is as follows: $y = 0.0 + 0.333 \times X_s + 0.333 \times X_n +$ $0.333 \times X_t$. For the relationship between year and temperature, the following contents can be obtained by repeating the above process. The formula of the model is as follows:

Note: ***, ** and * represent the significance level of 1%, 5% and 10% respectively

Table 7.3 Linear regression results analysis table

 $y = -0.36 + 0.009 \times X_{y}$.

7 . 1 . 4 *Conclusion and Analysis*

Through the above process, it can be seen that global temperature is strongly correlated with regions and years, and the specific relationship can be solved by linear regression model:

Global Temperature and Region: $y = 0.0 + 0.333 \times X_s + 0.333 \times X_n + 0.333 \times X_t$ Global temperature and Year: $y = -0.36 + 0.009 \times X_y$

7 . 2 The Influence of Other Factors on Temperature

7 . 2 . 1 *Data Preprocessing*

To further explore the impact of volcanic eruptions, forest fires and COVID-*19* on global temperatures, we need to separate these three periods into appropriate time nodes.

For volcanic eruptions, we selected the impact and the larger eruption of Mount Pinatubo in the Philippines to explore its impact on global temperatures. The eruption of Mount Pinatubo occurred in *1991*, and we use the *1991* and *1992* global temperature data as a boundary to explore further with the temperature data of the last *10* years.

As for forest fires, the long duration of bushfires in Australia has caused a very bad impact on the ecology. The bushfires in Australia have been extended from September *2019* to January *2020*. Taking this as the time node, we select the global temperature data during the bushfires and the following *8* months, a total of *12* months, as well as the data of *12* months before the bushfires for further exploration.

For the COVID-*19* outbreak from December *2019* to now, we selected the global average temperature in *2020* and *2021*, as well as the temperature data from *2013* to *2019* before the outbreak.

7 . 2 . 2 *Grey Prediction Model*

In order to test whether the above three events had an impact on the global temperature during the period, we used the grey prediction model in *6.2.2*, used the original data set before the event to predict the theoretical temperature at the time of the event, and then compared the real temperature data with it to observe the impact degree of the corresponding events.

The specific theoretical prediction results and the real values are compared as follows:

Figure 7.4 Comparison of monthly bushfire temperatures in Australia

Note:Due to the large number of selected months for COVID-*19*, the comparison between the specific theoretical data and the real data will be shown in the appendix.

Figure 7.5 A comparison of monthly COVID-19 temperature data

The data selected for volcanic eruption are in the dimension of year, so the data amount is small. Here, the table is used to display the data intuitively.

7 . 2 . 3 *Results and Analysis*

From the comparison between the theoretical forecast data and the real data, it can be seen that the Australian bushfire and the eruption of Mount Pinatubo in the Philippine

Year	Prediction of theory	The actual
1991	14.02	14.05
1992	14.1	14.18

Table 7.6 Comparison table of annual eruption temperature data of Mount Pinatubo

Islands both had a certain impact on the temperature conditions within a certain time range, resulting in a small increase in global temperature. The outbreak of the novel coronavirus has lowered global temperatures within a certain observation range, but the decrease is negligible. Therefore, we believe that the factors that have a certain influence on global temperature include stronger volcanic eruptions and long duration forest fires.

7 . 3 Analysis of Main Causes of Temperature Change

According to the above analysis in *7.2*, both volcanic eruptions and forest fires can cause a small increase in global temperature to some extent, while both can cause a sharp increase in carbon emissions. Therefore, we believe that carbon emissions are the main cause affecting global temperature. To do this, we collected nearly *70* years of global annual carbon emissions, and again correlated them with global temperatures to observe the results.

Note: ***, $\overline{}$ and $\overline{}$ represent the significance level of 1%, 5% and 10% respectively

Table 7.7 Significant value analysis table

As can be seen from the above table and the thermal map of correlation coefficient, the correlation between carbon emission and global temperature is very high, which just confirms the above conclusion. Therefore, we can infer that carbon emission is the main factor causing global temperature change.

Figure 7.8 Correlation coefficient heat map

7 . 4 Solution

The above situation shows that carbon emission is the main factor affecting global warming. Therefore, we propose the following countermeasures:

1. Strictly strengthen the protection of ecological environment, and deal with natural disasters in time to avoid tragedies.

2. Reduce the use of fossil fuels, continue to promote the popularization of new energy, so that every country can reduce carbon emissions.

3. Through exchanges and cooperation between countries, research and development of advanced energy-saving technologies, reduce the emission of harmful gases, reduce the harm of pollution to the atmosphere environment. In accordance with the principle of "common but differentiated responsibilities" set out in the Convention, countries have earnestly strengthened cooperation among themselves on climate change mitigation and related issues[7].

VIII. Evaluation of Model

8 . 1 The Advantages of Model and Paper

Reasonable assumptions: Based on extensive literature reading, this paper establishes a series of scientific assumptions through in-depth research and analysis of the problem, ignores some factors that have little impact on the results, simplifies the model and algorithm, and improves the operational efficiency of the model.

Result visualization: In this paper, MATLAB software was used to visualize the oper-

ation and related change rules of the relevant model, making the operation results of the model more intuitive.

Model generality: The classification model and correspondence analysis model established in the process of problem solving can be changed with different sample sets to adapt to different actual situations, and the model has good generality.

8 . 2 Disadvantages and Deficiencies of the Model

- **1.** For some temperature data divided according to different locations, the method is directly processed by adding and averaging, without further collecting real data for verification, so there are some loopholes in this method.
- **2.** The established model has not been simulated and verified, which has certain limitations.

IX. Memorandum

Dear Sir:

The problem of global warming is becoming more and more serious. Our team has carried out specific analysis and research based on the data provided, and obtained some valuable conclusions.

i.First, we do not agree that the rise in global temperatures in March 2022 is responsible for a larger increase than in the previous decade, based on a differential analysis of the data. There was no significant difference in temperature increase between the months and years.

ii. Secondly, after building the prediction model, we predicted the global temperature in 2050 and 2100, and found that it could not reach 20°C. Therefore, we do not agree that the global temperature will reach 20°C in 2050 or 2100. After further calculation through the two prediction models we have established, we conclude that this time node should be 2187 or 2215 years. And our prediction model has excellent accuracy.

iii. Global temperature is strongly correlated with time and location. After corresponding linear regression analysis, we establish linear equations of temperature and location and temperature and time respectively, which is helpful to further judge their relationship.

iV. After studying the impact of natural disasters on global temperature, we concluded that both forest fires and volcanic eruptions can cause a small increase in global temperature, while the impact of COVID-19 on global temperature is not significant. Here we believe that the main reason behind it is carbon emissions, so we conducted correlation analysis to confirm our conclusions and provide some measures to mitigate global warming.

The above are the findings of our team after research. I hope the models, analysis and conclusions mentioned above will be helpful to your work or research, and I also hope that human society can solve the problem of global warming as soon as possible.

Sincerely,

Team apmcm2205766

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I. Appendix

1 . 1 Global Arima

1 . 2 Global Grey Forecasting

1 . 3 Epidemic prediction

